

# C<sub>CHAPTER</sub> 14

## Additional Problems

### Solved Problems

14.1 The speed of a separately excited d.c. motor is controlled below base-speed by type-A chopper. The supply voltage is 220 V *dc*. The armature circuit has  $R_a = 0.5 \Omega$  and  $L_a = 10$  mH. The motor constant is  $K_v = 0.1$  V/rpm. Motor drives a constant torque load requiring an average armature current of 30 A. On the assumption of continuous armature current, determine:

- (a) range of speed control and
- (b) range of duty cycle.

**Sol.** Motor terminal voltage,

$$E_t = E_o = E_a + I_a \cdot R_a.$$

Minimum possible speed of d.c. motor is zero. This gives motor counter emf,  $E_a = 0$ .

$$\therefore \alpha E_s = E_o = 0 + I_a \cdot R_a.$$

$$\alpha \times 220 = 0 + 30 \times 0.5 = 15 \text{ V}$$

$$\therefore \alpha = \frac{15}{220} = 3/44.$$

Maximum possible value of duty cycle is 1.

$$\therefore \alpha E_s = E_a + I_a \cdot R_a.$$

$$1 \times 220 = kV \cdot N + 30 \times 0.5.$$

$$\therefore N = \frac{220 - 15}{0.10} = 2050 \text{ rpm.}$$

Therefore

(a) range of speed control is  $0 < N < 2050$  rpm and

(b) range of duty cycle,  $\frac{3}{44} < \alpha < 1$

14.2 A separated excited d.c. motor is fed from three phase six-pulse fully controlled bridge converter. The motor develops its full-load torque at a rated speed of 1800 rpm taking a rated current of 60 A at 440 V. The input to three-phase converter is from an ideal source of 50 Hz.

(a) Determine the *rms* value of line voltages input to the converter if motor runs at its rated conditions for delay angle  $\alpha = 0^\circ$ .

(b) What is the range of firing angles for a speed control of 1800 rpm to 900 rpm? The armature resistance is 0.5 ohm.

**Sol.** (a) We have, 
$$E_{dc\alpha} = \frac{3\sqrt{2} E}{\pi} \cos \alpha$$

At  $\alpha = 0^\circ, E_{dc\alpha} = 440 \text{ V}$

$\therefore 440 = \frac{3\sqrt{2} E}{\pi} \therefore E = 326 \text{ V.}$

(b) Back emf of motor at rated condition,

$$Eb_1 = 440 - 60 \times 0.5 = 410 \text{ V} = K \times 1800$$

Back emf at 900 rpm =  $Eb_2 = K \times 900$

Or 
$$\frac{Eb_2}{410} = \frac{K \times 900}{K \times 1800} = 1/2 \text{ or}$$

$$Eb_2 = \frac{410}{2} = 205 \text{ V.}$$

Hence of 900 rpm,

$$\begin{aligned} E_{dc\alpha} &= Eb_2 + I_a \cdot R_a = 205 + 60 \times 0.5 \\ &= 235 \end{aligned}$$

$\therefore$  Hence,  $235 = 1.35 \times 326 \cos \alpha$

$$\cos \alpha = 235 / 1.35 \times 326 = 0.534$$

$$= \cos 57.71^\circ$$

$\therefore \alpha = 57.71^\circ.$

$\therefore$  Range of firing delay angle is

$$\theta \leq \alpha \leq 57.710$$